

UNIFY: Unified Index for Range Filtered Approximate Nearest Neighbors Search

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ABSTRACT

This paper presents an efficient and scalable framework for Range Filtered Approximate Nearest Neighbors Search (RF-ANNS) over high-dimensional vectors associated with attribute values. Given a query vector q and a range $[l, h]$, RF-ANNS aims to find the approximate k nearest neighbors of q among data whose attribute values fall within $[l, h]$. Existing methods including pre-, post-, and hybrid filtering strategies that perform attribute range filtering before, after, or during the ANNS process, all suffer from significant performance degradation when query ranges shift. Though building dedicated indexes for each strategy and selecting the best one based on the query range can address this problem, it leads to index consistency and maintenance issues.

Our framework, called UNIFY, constructs a unified Proximity Graph-based (PG-based) index that seamlessly supports all three strategies. In UNIFY, we introduce SIG, a novel Segmented Inclusive Graph, which segments the dataset by attribute values. It ensures the PG of objects from any segment combinations is a sub-graph of SIG, thereby enabling efficient hybrid filtering by reconstructing and searching a PG from relevant segments. Moreover, we present Hierarchical Segmented Inclusive Graph (HSIG), a variant of SIG which incorporates a hierarchical structure inspired by HNSW to achieve logarithmic hybrid filtering complexity. We also implement pre- and post-filtering for HSIG by fusing skip list connections and compressed HNSW edges into the hierarchical graph. Experimental results show that UNIFY delivers state-of-the-art RF-ANNS performance across small, mid, and large query ranges.

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The source code, data, and/or other artifacts have been made available at <https://github.com/sjtu-dbgroun/UNIFY>.

1 INTRODUCTION

In recent years, Approximate Nearest Neighbors Search (ANNS) has drawn great attention for its fundamental role in data mining [25, 38], recommendation systems [36], and retrieval-augmented generation (RAG) [19], etc. Numerous ANNS methods [2, 7, 23, 26, 37, 41, 50] have been developed to efficiently retrieve similar unstructured objects (e.g., text, images, and videos) by indexing and searching their high-dimensional feature vectors [25]. However, ANNS fails to support many real-world scenarios where users need to filter objects not only by feature similarities but also by certain constraints. For example, Google Image Search allows users to upload an image and search for similar images within a specific period. Likewise, e-commerce platforms such as Amazon enable customers to find visually similar products within a price range.

The above queries can be formulated as the *range filtered approximate nearest neighbors search (RF-ANNS)* queries. Consider a vector dataset where each vector is associated with a numeric attribute (e.g., date, price, or quantity). Given a query vector q and a range $[l, h]$, RF-ANNS returns q 's approximate k nearest neighbors among the data whose attributes are within the range $[l, h]$. Several studies [33, 39, 40, 43, 47] have been carried out on the RF-ANNS problem, which can be categorized into the following three strategies based on when the attribute filtering is performed.

Strategy A: Pre-Filtering. This strategy performs ANNS after the attribute filtering. For example, Alibaba ADBV [43] integrates the pre-filtering strategy using a B-tree to filter attributes, followed by a linear scan on the raw vectors or PQ [16] codes. Milvus [39] partitions data by attributes and builds ANNS indexes for subsets. RF-ANNS is done by first filtering out partitions covering the query range, then performing ANNS on subset indexes. This strategy is efficient for small query ranges, but it does not scale well with larger ranges due to the linearly increasing overhead for scanning qualified vectors or indexes.

Strategy B: Post-Filtering. This strategy uses an ANNS index to find k' candidate vectors ($k' > k$), then filters by attributes to obtain the final top- k results. Vearch [20] and NGT [46] apply this strategy, which can be easily extended to popular ANNS indexes like HNSW [23] and IVF-PQ [16, 18]. This method is efficient for large query ranges. In the extreme case where the query range covers 100% of objects, RF-ANNS becomes equivalent to ANNS,

making post-filtering efficient. However, if the query range is small, the ANNS stage may struggle to collect enough qualified candidates, resulting in sub-optimal performance.

Strategy C: Hybrid Filtering. In Strategy A or B, an RF-ANNS query is decomposed into two sub-query systems for attribute filtering and ANNS processing. In contrast, Strategy C employs a single data structure to index and search vectors and attributes simultaneously. Several studies [10, 40] propose to employ state-of-the-art Proximity Graphs (PGs) [41], e.g., HNSW [23] and Vahama [10, 15], to implement Strategy C for ANNS with categorical filtration (searching similar vectors whose attributes match a label). The recent study SeRF [52] is the first work implementing Strategy C with PGs for RF-ANNS. It compresses multiple HNSWs into a hybrid index. RF-ANNS is carried out by reconstructing and searching an HNSW index only containing objects in the query range. SeRF achieves state-of-the-art performance on query ranges from 0.3% to 50%. However, it lags behind Strategy A and B for smaller and larger ranges due to the overhead of HNSW reconstruction. Additionally, SeRF lacks support for incremental data insertion, limiting its use in scenarios with new object arrivals.

Problems and Our Solutions. As discussed above, existing methods suffer from two challenges: *sub-optimal performance when query range shifts* and *lack of incremental data insertion support*. A trivial solution is to build dedicated indexes for each strategy and adaptively select the best one based on the query range. However, this requires extra effort to ensure data consistency across multiple indexes, leading to high maintenance costs [40]. To tackle these problems, we propose a UNIFY framework combining Strategies A, B, and C into a unified PG-based index supporting incremental insertion. UNIFY is designed to enhance RF-ANNS performance by prioritizing the following key objectives: (O1) enabling efficient hybrid filtering, (O2) supporting incremental index construction, (O3) integrating pre- and post-filtering strategies, and (O4) implementing a range-aware selection of search strategies. The key techniques in UNIFY to achieve these objectives include:

(1) *Segmented Inclusive Graph (SIG) (O1).* For efficient hybrid filtering, we introduce a novel graph family named SIG. SIG segments the dataset based on attribute values and theoretically guarantees that the PG of objects from any combination of segments is a sub-graph of SIG. For example, segment a dataset $\mathcal{D}$ into three subsets $\mathcal{D}_1$, $\mathcal{D}_2$, and $\mathcal{D}_3$, and let $\mathbb{G}(X)$ denote the PG constructed on dataset X . The PGs $\mathbb{G}(\mathcal{D}_1)$, $\mathbb{G}(\mathcal{D}_2)$, $\mathbb{G}(\mathcal{D}_1 \cup \mathcal{D}_2)$, $\dots$, $\mathbb{G}(\mathcal{D}_1 \cup \mathcal{D}_2 \cup \mathcal{D}_3)$ are all included in SIG. This characteristic allows us to reconstruct and search a small PG from relevant segments intersected with the query range to enhance RF-ANNS performance.

(2) *Hierarchical Segmented Inclusive Graph (HSIG) (O1 & O2).* Based on SIG, we introduce HSIG, a hierarchical graph inspired by HNSW. Similar to HNSW, HSIG is built incrementally. Besides, as a variant of SIG, HSIG can approximately ensure that the HNSW of objects from any combination of segments is a sub-graph of HSIG. By reconstructing and searching an HNSW for relevant segments, we achieve $O(\log(n'))$ RF-ANNS time complexity, where n' is the number of objects in those segments.

(3) *Fusion of skip list connections (O3).* The skip list is a classic attribute index optimized for one-dimensional key-value lookup and range search (see Section 2 for more details). We observe that the skip list shares a similar hierarchical structure with our HSIG.

Inspired by this, we fuse the skip list connections that reflect the order of attribute values into the hierarchical graph structure to form a hybrid index. By navigating these skip list connections, we can efficiently select objects within the query range, thereby implementing efficient pre-filtering.

(4) *Global edge masking (O3).* Recall that post-filtering relies on a global ANNS index over the entire dataset. HSIG ensures that the global HNSW is approximately a sub-graph of it, meaning that each node's global HNSW edges are included within its HSIG edges. We employ an edge masking algorithm to mark the global HNSW edges with a compact bitmap. Navigated by these bitmap-marked edges, we can perform ANNS over the global HNSW to efficiently support post-filtering.

(5) *Range-aware search strategy selection (O4).* Inspired by the effectiveness of Strategies A, B, and C for different query ranges, we developed a heuristic for range-aware strategy selection. Let Y denote the cardinality of objects that fall within the query range, our heuristic is: use Strategy A for $Y \leq \tau_A$, Strategy B for $Y \geq \tau_B$, and Strategy C for $\tau_A < Y < \tau_B$. Here, τ_A and τ_B serve as thresholds to distinguish the ranges for which each strategy is most effective, and they can be derived from historical data statistics. In this paper, we run a set of sample queries to collect statistics and determine τ_A and τ_B . Experimental results show that this heuristic is effective.

Contributions. Our contributions are summarized as follows:

- We introduced SIG, a novel graph family that segments the dataset based on attribute values, ensuring efficient hybrid filtering by allowing the reconstruction and search of a PG from relevant segments.
- We developed HSIG, a novel hybrid index that supports efficient hybrid filtering with logarithmic time complexity for RF-ANNS and enables incremental data insertion.
- We integrated novel auxiliary structures, including skip list connections and edge masking bitmaps, into HSIG to support both pre- and post-filtering strategies. To the best of our knowledge, HSIG is the first index supporting pre-, post-, and hybrid filtering simultaneously.
- Experiments on real-world datasets demonstrate that our approach significantly outperforms state-of-the-art methods for query ranges from 0.1% to 100% by up to 2.29 times.

2 PRELIMINARIES

2.1 Problem Definition

This paper considers a dataset $\mathcal{D}$ with attributed vectors and nearest neighbors search (NNS) with attribute constraints. Specifically, let A be an attribute (e.g., date, price, or quantity). We use $v[A]$ to denote the attribute value associated with vector v . The range filtered nearest neighbors search (RF-NNS) problem is defined as:

DEFINITION 1 (RF-NNS). *Given a dataset $\mathcal{D}$ of n attributed vectors $\{v_1, v_2, \dots, v_n\}$, a distance function $\Gamma(\cdot, \cdot)$, and a query $Q = (q, [l, h], k)$ with q as the query vector, an integer k from 1 to n , and $[l, h]$ a real-valued query range, RF-NNS returns the k NN($q, \mathcal{R}$), a subset of $\mathcal{R} = \{v \mid v \in \mathcal{D} \text{ and } l \leq v[A] \leq h\}$. For any $o \in k$ NN($q, \mathcal{R}$) and any $u \in \mathcal{R} \setminus k$ NN($q, \mathcal{R}$), it holds that $\Gamma(o, q) < \Gamma(u, q)$. If $|\mathcal{R}| < k$, all objects in $\mathcal{R}$ are returned.*

Algorithm 1: ANNSearch

Input : $\mathbb{G}$: HNSW layer; q : query vector; ep : entry point; k : an integer.

Output: q 's approximate k nearest neighbors on $\mathbb{G}$.

```
1 push  $ep$  to the min-heap  $cand$  in the order of distance to  $q$ ;  
2 push  $ep$  to the max-heap  $ann$  in the order of distance to  $q$ ;  
3 mark  $ep$  as visited;  
4 while  $|cand| > 0$  do  
5    $o \leftarrow$  pop the nearest object to  $q$  in  $cand$ ;  
6    $u \leftarrow$  the furthest object to  $q$  in  $ann$ ;  
7   if  $\Gamma(o, q) > \Gamma(u, q)$  then break;  
8   foreach  $unvisited\ v \in \mathbb{G}[o]$  do  
9     mark  $v$  as visited;  
10     $u \leftarrow$  the furthest object to  $q$  in  $ann$ ;  
11    if  $\Gamma(v, q) < \Gamma(u, q)$  or  $|ann| < k$  then  
12      push  $v$  to  $cand$  and  $ann$ ;  
13      if  $|ann| > k$  then pop  $ann$ ;  
14 return  $ann$ ;
```

Due to the "curse of dimensionality" [14], exact NNS in high-dimensional space is inefficient [21]. As a result, most research focuses on approximate nearest neighbors search (ANNS), which reports approximate results with an optimized recall. Similarly, this paper studies the RF-ANNS problem, which returns an approximate result set $kNN'(q, \mathcal{R})$ with an optimized recall:

$$recall = \frac{|kNN'(q, \mathcal{R}) \cap kNN(q, \mathcal{R})|}{\min(k, |\mathcal{R}|)}. \quad (1)$$

2.2 Proximity Graph

A Proximity Graph (PG) [41] treats a vector as a graph node, with connections built based on vector proximity. Various greedy heuristics are proposed to navigate the graph for ANNS [41]. In the following, we introduce two PGs related to our work.

k Nearest Neighbor Graph ($kNNG$) [29]. Given a dataset $\mathcal{D}$, a $kNNG$ is built by connecting each vector v to its k nearest neighbors, $kNN(v, \mathcal{D} \setminus \{v\})$. $kNNG$ limits the number of edges per node to at most k , making it suitable for memory-constrained environments. However, $kNNG$ focuses on local connections and does not guarantee global connectivity, leading to sub-optimal performance compared to state-of-the-art PGs such as HNSW [23].

Hierarchical Navigable Small World Graph (HNSW) [23]. HNSW is inspired by the 1D probabilistic structure of the skip list [32], where each layer is a linked list ordered by 1D values. The bottom layer includes all objects, while the upper layers contain progressively fewer objects. HNSW extends this structure by replacing linked lists with PGs, enabling efficient hierarchical search. The hierarchical structure of HNSW is similar to that in Figure 4. As shown in Algorithm 1, HNSW uses a greedy approach to find the kNN for query vector q in each layer. The neighbors of each node v_i in a given layer $\mathbb{G}$ are stored in adjacency lists $\mathbb{G}[v_i]$. The search starts at an entry point ep , the most recently inserted vector at the topmost layer [23]. It repeatedly selects the nearest object o to

Algorithm 2: HierarchicalANNS

Input : $\mathbb{H}$: HNSW; q : query vector; ep : entry point; ef : enlarge factor; k : an integer.

Output: q 's approximate k nearest neighbors.

```
1  $L \leftarrow$  max level of  $\mathbb{H}$ ;  
2 foreach  $L \geq i \geq 1$  do  
3   /* Search the  $i$ -th layer  $\mathbb{H}^i$ . */  
4    $ann \leftarrow$  ANNSearch( $\mathbb{H}^i, q, ep, 1$ );  
5    $ep \leftarrow$  the nearest object to  $q$  in  $ann$ ;  
6   /* Search the bottom layer  $\mathbb{H}^0$ . */  
7    $ann \leftarrow$  ANNSearch( $\mathbb{H}^0, q, ep, ef$ );  
8 return top- $k$  nearest objects to  $q$  in  $ann$ ;
```

Algorithm 3: InsertLayer

Input : $\mathbb{G}$: HNSW layer; v : the object to insert; ep : entry point; M : the maximum degree; $efCons$: number of candidate neighbors.

Output: the updated graph.

```
1  $ann \leftarrow$  ANNSearch( $\mathbb{G}, v, ep, efCons$ )  
2  $\mathbb{G}[v] \leftarrow$  Prune( $v, ann, M$ )  
3 foreach  $o \in \mathbb{G}[v]$  do  
4   add  $v$  to  $\mathbb{G}[o]$ ;  
5   if  $|\mathbb{G}[o]| > M$  then  $\mathbb{G}[o] \leftarrow$  Prune( $o, \mathbb{G}[o], M$ );  
6 return  $\mathbb{G}$ ;
```

q from $cand$ (Line 5), adds o 's unvisited neighbors to $cand$ (Lines 8–12), and updates ann (Lines 11–13). The search ends when all nodes in $cand$ are farther from q than those in ann . As shown in Algorithm 2, the hierarchical search in HNSW begins at a coarse layer to identify promising regions and progressively descends to finer layers for detailed exploration. To improve accuracy, Algorithm 2 uses the parameter ef ($ef > k$), initially exploring ef neighbors to broaden the search region, and finally returns the top- k results.

HNSW is built incrementally based on Algorithm 3. When inserting a new object v into an HNSW layer, the process begins by searching for its top $efCons$ nearest neighbors using the ANNSearch algorithm (Line 1). The Prune heuristic is then applied to limit v 's connections to a maximum of M (Line 2). The value of M , typically set between 5 and 48 [23], balances accuracy and efficiency, with its optimal value determined experimentally. The Prune method initially sorts v 's candidate neighbors by distance. For each candidate r , if a neighbor e satisfies $\Gamma(v, r) > \Gamma(e, r)$, r is pruned. Otherwise, an edge between v and r is inserted. The process continues until v has M neighbors. Additionally, v is added to the neighbor lists of its identified neighbors, and the Prune method is applied to each neighbor to maintain the M -neighbor limit (Lines 3–5). The Prune strategy prevents the graph from becoming overly dense, ensuring efficient navigation. HNSW achieves state-of-the-art ANNS time complexity of $O(\log n)$ [41] and demonstrates top-tier practical performance indicated by various benchmarks [3, 21, 41]. It also serves as the backbone for various vector databases such as Pinecone [31], Weaviate [42], and Milvus [39].

3 SEGMENTED INCLUSIVE GRAPH

We aim to develop a PG-based index that integrates three search strategies and supports incremental construction. Section 3.1 introduces the Segmented Inclusive Graph (SIG), a novel graph family that leverages attribute segmentation and inclusivity for hybrid filtering. Section 3.2 explores the challenges of constructing an SIG using the basic PG structure k NNG and presents practical solutions.

3.1 SIG Overview

Attribute Segmentation. Given a dataset of n objects, RF-ANNS is concerned only with the n' objects within the query range, where $n' \leq n$. To efficiently filter out the qualified objects, we employ the attribute segmentation method to reduce the search space. Assuming that the attribute distribution remains stable, we first sample objects from the dataset and sort them by their attribute values, then apply an equi-depth histogram [30] to partition them. The histogram bin boundaries define the attribute intervals for each segment, partitioning the dataset into disjoint subsets with similar sizes for further indexing.

Graph Inclusivity and SIG. After attribute segmentation, we focus on designing a graph for efficient hybrid filtering. Since a query range intersects a few segments, a straightforward approach is to independently build PGs for each segment. For an RF-ANNS query, we search the local PGs in intersected segments and merge the results for the global k NN. However, this method results in search time increasing linearly with the number of intersected segments. State-of-the-art PGs offer an ANNS time complexity of $O(\log n)$, suggesting sub-linear search time growth with the number of intersected segments. For example, with S segments, searching multiple PGs scales as $O(S \log(\frac{n}{S}))$, while searching a single PG containing all objects scales as $O(\log n)$. The ratio between them is $S \left(1 - \frac{\log S}{\log n}\right)$. Since $1 < S \ll n$, this ratio is greater than 1 but less than S , indicating that searching across multiple PGs is less efficient than searching a single PG containing all objects.

Inspired by this, we introduce a novel graph family known as the Segmented Inclusive Graph (SIG). An SIG ensures that the PG of any segment combination is included in (i.e., is a sub-graph of) the SIG. Leveraging this characteristic, termed *graph inclusivity*, allows efficient hybrid filtering by reconstructing and searching the smaller PG of a few segments covering the query range. Below, we introduce the formal definitions of graph inclusivity and SIG.

DEFINITION 2 (GRAPH INCLUSIVITY AND SEGMENTED INCLUSIVE GRAPH). Let $\mathbb{G}(X)$ denote a PG constructed over the dataset X . Given a dataset $\mathcal{D}$ segmented into S disjoint subsets $\mathcal{P} = \{\mathcal{D}_1, \mathcal{D}_2, \dots, \mathcal{D}_S\}$, a segmented inclusive graph $\text{SIG}(\mathcal{D})$ is a type of graph that possesses the property of graph inclusivity defined as

$$\forall r \in \{1, 2, \dots, S\}, \forall C \in \mathcal{P}^{(r)}, \mathbb{G}\left(\bigcup_{e \in C} e\right) \subseteq \text{SIG}(\mathcal{D}), \quad (2)$$

where $\mathcal{P}^{(r)}$ denotes all possible combinations of r elements from $\mathcal{P}$.

EXAMPLE 1. Assume that $\mathcal{P} = \{\mathcal{D}_1, \mathcal{D}_2, \mathcal{D}_3\}$, we have $\mathcal{P}^{(2)} = \{\{\mathcal{D}_1, \mathcal{D}_2\}, \{\mathcal{D}_1, \mathcal{D}_3\}, \{\mathcal{D}_2, \mathcal{D}_3\}\}$. For one of the possible combinations $C = \{\mathcal{D}_1, \mathcal{D}_2\}$, we have $\bigcup_{e \in C} e = \mathcal{D}_1 \cup \mathcal{D}_2$. It holds that $\mathbb{G}(\mathcal{D}_1 \cup \mathcal{D}_2) \subseteq \text{SIG}(\mathcal{D})$.

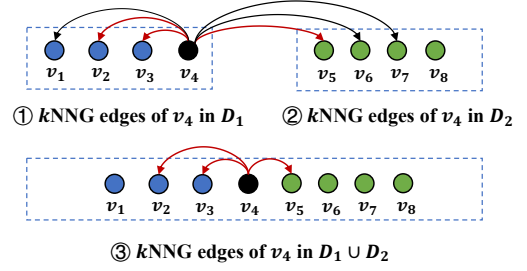


Figure 1: Build multiple k NNGs exhaustively ($k = 3$).

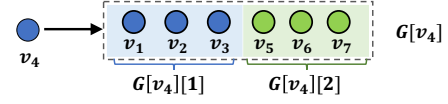


Figure 2: Example of the segmented adjacency list ($k = 3$).

Based on Definition 2, we derive an exhaustive SIG construction algorithm: build PGs for all segment combinations and merge them into a single graph. While it guarantees graph inclusivity, it faces significant computational challenges. With S segments, the number of combinations is $\sum_{i=1}^S \binom{S}{i} = 2^S - 1$, and the space complexity of SIG scales as $O(2^S - 1)$, making the construction of all PGs both computationally and spatially prohibitive¹. Thus, we propose a space-efficient SIG index that scales as $O(S)$ in the next section.

3.2 SIG- k NNG

In this section, we conduct a case study on k NNG to demonstrate the limitations of the exhaustive method. Then, we introduce SIG- k NNG, a novel graph structure that guarantees inclusivity without exhaustively building all possible k NNGs.

Limitation of the Exhaustive Method. For each object v in a dataset $\mathcal{D}$, constructing a k NNG involves adding a directed edge (v, o) for each object $o \in kNN(v, \mathcal{D} \setminus \{v\})$. When the dataset is divided into S subsets by attribute segmentation, the exhaustive method requires running the construction algorithm $2^S - 1$ times. Figure 1 illustrates an example. Here, the dataset $\mathcal{D}$ is divided into two subsets $\mathcal{D}_1 = \{v_1, v_2, v_3, v_4\}$ and $\mathcal{D}_2 = \{v_5, v_6, v_7, v_8\}$. We need to build k NNGs ($k=3$) for $\mathcal{D}_1$, $\mathcal{D}_2$, and $\mathcal{D}_1 \cup \mathcal{D}_2$, respectively. Such exhaustive construction is unnecessary, as the k NN of a union is inherently within the individual k NN sets. For example, all objects in $kNN(v_4, \mathcal{D}_1 \cup \mathcal{D}_2)$ can be found in $kNN(v_4, \mathcal{D}_1) \cup kNN(v_4, \mathcal{D}_2)$. In other words, v_4 's three edges in graph ③ are already included in graphs ① and ②, making the construction of graph ③ redundant.

Structure of SIG- k NNG. Inspired by the prior observations, we introduce SIG- k NNG, a novel graph structure that achieves inclusivity without the need for exhaustive k NNG construction. SIG- k NNG uses a segmented adjacency list to store the outgoing edges for each object in the graph. As illustrated in Figure 2, given a dataset $\mathcal{D}$ segmented into S subsets $\mathcal{D}_1, \dots, \mathcal{D}_S$, the adjacency list for any object

¹In fact, for RF-ANNS, we only need to consider continuous segments, with potential combinations totaling $0.5(n^2 - n)$, which is also prohibitive. Since the conclusions in this paper apply to both all segment combinations and continuous ones, we discuss the harder scenario, i.e., all segment combinations, to maintain generality.

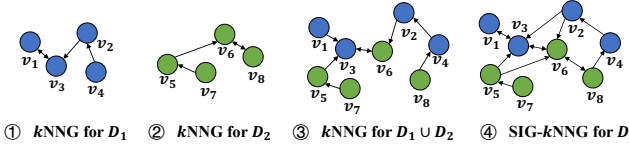


Figure 3: Illustration of SIG-kNNG’s inclusivity ($k = 1$).

v is divided into S chunks. For example, the full adjacency list $\mathbb{G}[v_4]$ of object v_4 is segmented into two chunks $\mathbb{G}[v_4][1]$ and $\mathbb{G}[v_4][2]$. The i -th chunk stores only v ’s k NN within $\mathcal{D}_i$. Based on this design, to add SIG-kNNG edges for v , we perform k NN searches S times to find its neighbors in each subset, instead of searching $2^S - 1$ times across all subset combinations. In the following, we introduce the formal definition of SIG-kNNG and prove that SIG-kNNG can exactly guarantee inclusivity.

DEFINITION 3 (SIG-kNNG). Given a dataset $\mathcal{D}$ segmented into S disjoint subsets $\mathcal{D}_1, \mathcal{D}_2, \dots, \mathcal{D}_S$, the SIG-kNNG on $\mathcal{D}$ is defined as $\mathbb{F}_k(\mathcal{D}) = (V_{\mathbb{F}}, E_{\mathbb{F}})$, where $V_{\mathbb{F}} = \mathcal{D}$ and $E_{\mathbb{F}} = \bigcup_{v \in \mathcal{D}} \bigcup_{i=1}^S E_i^k(v)$. Here, $E_i^k(v)$ is the set of edges based on the i -th chunk of v ’s adjacency list, defined as $E_i^k(v) = \{(v, o) \mid o \in kNN(v, \mathcal{D}_i \setminus \{v\})\}$.

Inclusivity of SIG-kNNG. We first present the following lemma, which shows that the k NN of a union is inherently included in the individual k NN sets.

LEMMA 1. Given r disjoint datasets $\mathcal{D}_1, \mathcal{D}_2, \dots, \mathcal{D}_r$ and their union set $\mathcal{U} = \bigcup_{i=1}^r \mathcal{D}_i$, it holds that $\forall v \in \mathcal{U}, kNN(v, \mathcal{U} \setminus \{v\}) \subseteq \bigcup_{i=1}^r kNN(v, \mathcal{D}_i \setminus \{v\})$.

Based on Lemma 1, we derive the inclusivity of SIG-kNNG, as presented in Theorem 1. The proof is omitted here for brevity, as it is straightforward to follow.

THEOREM 1. Let $\mathbb{G}_k(X)$ and $\mathbb{F}_k(X)$ denote a k NNG and SIG-kNNG for dataset X , respectively. Given a dataset $\mathcal{D}$ segmented into S disjoint subsets $\mathcal{D}_1, \mathcal{D}_2, \dots, \mathcal{D}_S$, it follows that SIG-kNNG is a segmented inclusive graph. Specifically, for any r distinct integers $i_1, i_2, \dots, i_r$ chosen from $[1, S]$ with $1 \leq r \leq S$, we have $\mathbb{G}_k(\mathcal{U}) \subseteq \mathbb{F}_k(\mathcal{D})$, where $\mathcal{U} = \bigcup_{j=1}^r \mathcal{D}_{i_j}$.

EXAMPLE 2. Figure 3 demonstrates the inclusivity of SIG-kNNG. Given a dataset $\mathcal{D} = \{v_1, v_2, \dots, v_8\}$, we assume the attribute of v_i is i for simplicity. The attribute space $[1, 8]$ is divided into two disjoint segments $[1, 5]$ and $[5, 8]$, leading to two subsets $\mathcal{D}_1 = \{v_1, v_2, v_3, v_4\}$ and $\mathcal{D}_2 = \{v_5, v_6, v_7, v_8\}$. Graphs ①~③ represent the k NNGs for $\mathcal{D}_1$, $\mathcal{D}_2$, and $\mathcal{D}_1 \cup \mathcal{D}_2$, and the SIG-kNNG for $\mathcal{D}$ is displayed in graph ④. As illustrated, all three k NNGs are sub-graphs of the SIG-kNNG.

4 HIERARCHICAL SEGMENTED INCLUSIVE GRAPH

SIG-kNNG offers an efficient approach to build an SIG with segmented adjacency lists. Though it theoretically guarantees inclusivity, the underlying k NNG is not competitive with state-of-the-art PGs like HNSW [23]. Additionally, SIG-kNNG lacks support for incremental insertion. In this section, we expand the basic idea of SIG-kNNG, introducing the Hierarchical Segmented Inclusive

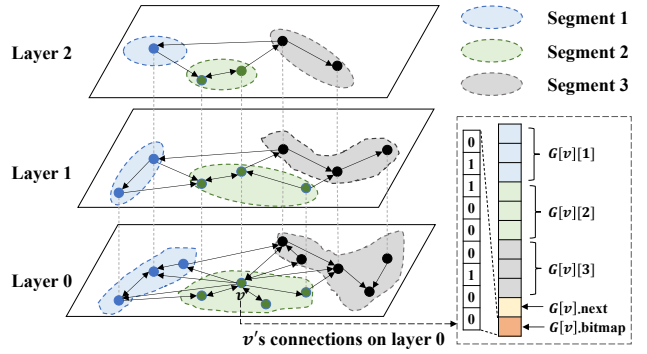


Figure 4: Illustration of HSiG.

Graph (HSiG), which uses HNSW as a building block to achieve incremental construction and a logarithmic search complexity.

Figure 4 provides an overview of HSiG, showcasing a hierarchical structure that follows the structure of HNSW and skip lists. HSiG is a unified structure that indexes both vectors and attributes by leveraging the strengths of vector-oriented HNSW and attribute-oriented skip lists. For vector indexing, HSiG organizes the outgoing edges of each object into chunks based on attribute segmentation, inspired by SIG-kNNG. Each chunk contains the edges of an HNSW for the corresponding segment. Thus, the backbone graph of HSiG can be seen as a set of HNSWs constructed for different segments (e.g., the three HNSWs with different colors in Figure 4), which are mutually connected with additional edges to ensure inclusivity. Additionally, we incorporate the skip list into the backbone graph to index attributes for efficient pre-filtering and introduce a compact auxiliary structure to optimize post-filtering. The structure and algorithms are detailed in Sections 4.1 and 4.2.

4.1 HSiG Construction

In this section, we describe the core structures of HSiG for hybrid, pre-, and post-filtering sequentially. Then, we integrate them to introduce the complete insertion algorithm.

Backbone Graph for Hybrid Filtering. Based on Theorem 1, we present HSiG’s backbone graph, which is designed to ensure inclusivity regarding HNSW and support efficient hybrid filtering. As depicted in Algorithm 3, when inserting a new object v into an HNSW layer, the core operation involves finding v ’s $efCons$ nearest neighbors and establishing up to M connections. This procedure is similar to k NNG’s construction, which finds k NN and establishes at most k connections. Therefore, we use the segmented adjacency list introduced by SIG-kNNG to guarantee the inclusivity for all possible HNSW connections. With S segments, connections are stored in S chunks, with a maximum degree of M per chunk. The values of S and M are experimentally determined, with default values set to 8 and 16, respectively. Since each chunk contains the HNSW connections in the corresponding segment, the objects and connections in chunk j form a sub-graph $\mathbb{G}_j$ of the backbone graph in HSiG. When inserting object v that is located in segment i , Algorithm 4 outlines how to build v ’s connections in segment j at an HSiG layer. First, we search for v ’s $efCons$ nearest neighbors in $\mathbb{G}_j$ (Line 1) using $ANNSearch$ (Algorithm 1), then select up to M

Algorithm 4: BackboneConnectionsBuild

Input : $\mathbb{G}$: HSIG layer; ep : entry point; v : the object to insert; i : index of the segment that $v[A]$ belongs to; j : index of the segment to insert; M : the maximum degree; $efCons$: number of candidate neighbors.

Output: v 's approximate nearest neighbors in $\mathbb{G}_j$ (a sub-graph of $\mathbb{G}$ with only nodes and edges in segment j).

```

1  $ann \leftarrow \text{ANNSearch}(\mathbb{G}_j, v, ep, efCons);$ 
2 foreach  $o \in \text{Prune}(v, ann, M)$  do
3   add  $(v, o)$  to  $\mathbb{G}[v][j]$ ;
4   add  $(o, v)$  to  $\mathbb{G}[o][i]$ ;
5   if  $|\mathbb{G}[o][i]| > M$  then
6      $\mathbb{G}[o][i] \leftarrow \text{Prune}(o, \mathbb{G}[o][i], M);$ 
7 return  $ann;$ 
```

neighbors using the *Prune* algorithm. For each neighbor o , we establish mutual connections between v and o within their respective segments (Lines 2–4). If the number of neighbors of o in segment i exceeds M , we apply the *Prune* algorithm to discard the extra neighbors (Lines 5–6). This algorithm guarantees the approximate inclusivity of HSIG, as demonstrated in Section 5.4.

Fusing Skip List Connections for Pre-Filtering. For small-range RF-ANNS queries, pre-filtering with an attribute index typically outperforms PG-based methods. This is because PGs prioritize vectors over attributes, making it difficult to filter candidates within the query range. For instance, in the extreme case of a query range containing only one object, using an attribute index to quickly locate the target object is optimal. Thus, we propose fusing an attribute index into the graph structure for effective pre-filtering. As described in Section 2, the skip list is a popular index for efficient 1D key-value lookups and range searches, sharing a hierarchical structure similar to HNSW and HSIK. Inspired by this, we integrate the skip list into the backbone graph of HSIK to form a unified index. Navigated by skip list connections, we can efficiently locate and linearly search objects within the query range. As shown in Figure 4, we use an extra connection $\mathbb{G}[v].next$ to store the ID of v 's successor object in the skip list. After inserting an object into the backbone graph via Algorithm 4, we search for its successor in the skip list and store it in $\mathbb{G}[v].next$.

Global Edge Masking for Post-Filtering. For large-range queries, post-filtering with a pure ANNS index is preferable. We use a global HNSW over the entire dataset to support post-filtering. Due to inclusivity, the global HNSW is (approximately) a sub-graph of HSIK. We apply a global edge pruning method to identify these HNSW edges from HSIK edges and use a compact bitmap to mask the unused edges. Since each segment's sub-graph has a maximum degree of M , we similarly limit the connections in the global graph to a maximum of M . This procedure is detailed in Algorithm 5. First, we obtain the object v 's connections in all segments and select M connections using the *Prune* algorithm (Line 1). Next, we create a bitmap whose size equals the number of v 's neighbors in all segments and set the positions of v 's M neighbors to 1 (Line 2). For each neighbor o in the M neighbors (Line 3), if v is also a

Algorithm 5: GlobalEdgeMasking

Input : $\mathbb{G}$: HSIK layer; v : the object to insert; M : the maximum degree.

Output: the updated graph.

```

1  $\mathcal{N} \leftarrow \text{Prune}(v, \mathbb{G}[v], M);$ 
2  $\mathbb{G}[v].\text{bitmap} \leftarrow \text{generate bitmap with } \mathcal{N};$ 
3 foreach  $o \in \mathcal{N}$  do
4   if  $v \in \mathbb{G}[o]$  then
5      $pos \leftarrow v$ 's position in  $\mathbb{G}[o]$ ;
6      $\mathbb{G}[o].\text{bitmap}[pos] \leftarrow 1;$ 
7     if  $\text{sum}(\mathbb{G}[o].\text{bitmap}) > M$  then
8        $\mathcal{N}' \leftarrow \text{Prune}(o, \mathbb{G}[o], M);$ 
9        $\mathbb{G}[o].\text{bitmap} \leftarrow \text{update bitmap with } \mathcal{N}';$ 
10 return  $\mathbb{G};$ 
```

neighbor of o , set the position of v in o 's bitmap to 1 (Lines 4–6). Then, we update the bitmap of o (Lines 7–9).

Complete Insertion Algorithm. As aforementioned, the adjacency list of a node in HSIK consists of (1) several chunks for backbone graph connections, (2) a skip list connection, and (3) a bitmap for global connections. The bottom-right of Figure 4 illustrates an example. Here, $\mathbb{G}[v][i]$ is the backbone graph connections of v in the i -th segment, $\mathbb{G}[v].next$ stores the ID of v 's successor in the skip list, and $\mathbb{G}[v].\text{bitmap}$ stores the global edge masks.

Next, we present the complete insertion algorithm for constructing an HSIK. The HSIK structure consists of a set of HNSWs for different segments, augmented with auxiliary structures for pre- and post-filtering. Construction involves three main steps: building the HNSW in each segment, adding skip list connections, and applying global edge masking. Each step is performed hierarchically and incrementally, as outlined in Algorithm 6. First, we find the segment to which object v belongs (Line 1). The maximum layer level of v is randomly assigned using an exponentially decaying probability distribution normalized by m_L (Line 2; see [23] for details). We then traverse all segments (Line 3) to sequentially build the HNSW $\mathbb{H}\mathbb{G}_j$ in each segment j , determining its maximum level L and entry point ep (Lines 4–5). For each layer l from L to $level + 1$, we use *ANNSearch* (Algorithm 1) to find the nearest neighbor ep of v in $\mathbb{H}\mathbb{G}_j^l$, where $\mathbb{H}\mathbb{G}_j^l$ denotes layer l in $\mathbb{H}\mathbb{G}_j$ (Lines 6–7). Then, for each layer l from $level$ to 0, we employ *BackboneConnectionsBuild* (Algorithm 4) to insert v into $\mathbb{H}\mathbb{G}_j^l$, using its nearest neighbor as the entry point for the next layer (Lines 8–10). After building $\mathbb{H}\mathbb{G}_j$, we update its entry point if necessary (Line 11), ensuring the first object in the topmost layer serves as the entry. Next, v is inserted into the skip list using the method in [32] (Line 12). Finally, we use *GlobalEdgeMasking* (Algorithm 5) to mask unnecessary edges for post-filtering from layer 0 to $level$ (Lines 13–14).

4.2 Search on HSIK

To adapt to different query ranges, we propose three search strategies and a range-aware search strategy selection method.

Strategy A (Pre-Filtering). Navigated by the hierarchical skip list connections, we can quickly reach the bottom layer to identify the

Algorithm 6: HSIInsert

Input : $\mathbb{HG}$: HSI; v : the object to insert; S : number of segments; M : the maximum degree; $efCons$: number of candidate neighbors.

Output: the updated HSI.

```

1  $i \leftarrow \text{ComputeSegmentId}(v[A]);$ 
2  $level \leftarrow \lfloor -\ln(\text{unif}(0 \dots 1) \cdot m_L) \rfloor;$ 
3 foreach  $1 \leq j \leq S$  do
4    $L \leftarrow$  the max level of  $\mathbb{HG}_j$ ;
5    $ep \leftarrow$  the entry point of  $\mathbb{HG}_j$ ;
6   foreach  $L \geq l \geq level + 1$  do
7      $ep \leftarrow \text{ANNSearch}(\mathbb{HG}_j^l, v, ep, 1);$ 
8   foreach  $level \geq l \geq 0$  do
9      $ann \leftarrow \text{BackboneConnectionsBuild}(\mathbb{HG}_j^l, ep, v, i, j,$ 
10       $M, efCons);$ 
11      $ep \leftarrow$  nearest object to  $v$  in  $ann$ ;
12   update graph entry for  $\mathbb{HG}_j$  if necessary;
13 add skip list connections for  $v$  in layers  $0 \dots level$ ;
14 foreach  $0 \leq l \leq level$  do
15    $\mathbb{HG}^l \leftarrow \text{GlobalEdgeMasking}(\mathbb{HG}^l, v, M);$ 
16 return  $\mathbb{HG}$ ;
```

first object whose attribute value falls within the query range. From there, a linear search is performed to collect the query vector's k NN among those vectors with qualified attribute values. This method is straightforward, so pseudocode is omitted.

Strategy B (Post-Filtering). We employ the hierarchical search scheme in Algorithm 2 for ANNS, followed by filtering objects within the query range. ANNS is performed over a global HNSW with edges marked by bitmaps. During the search, only outgoing edges marked as 1 in an object's bitmap are considered. The search retrieves the top- ef nearest neighbors ($ef > k$) in the bottom layer, after which attribute filtering is applied to obtain the top- k results.

Strategy C (Hybrid Filtering). We perform hybrid filtering by reconstructing and searching the HNSW of segments covering the query range. The search follows the hierarchical scheme in Algorithm 2, starting from the topmost entry point of graphs in all segments. Since each object has M connections per segment, and assuming there are S' segments intersecting the query range, this requires visiting MS' neighboring nodes, leading to a large search space and high computational complexity. Thus, we introduce the search parameter m to reconstruct a HNSW with a maximum degree of m at runtime. We propose two neighbor selection strategies to select m neighbors from MS' connections: (1) compute distances between node v and its neighbors across all S' segments, then select the top- m neighbors by sorting them by distance; and (2) select the top- $(\lceil m/S' \rceil)$ neighbors from each chunk of the adjacency list. Since neighbors in each chunk are naturally ordered by distance to v upon acquisition via ANNSearch , we simply take the first $\lceil m/S' \rceil$ objects. We adopt the second strategy as the default, based on experimental results in Section 5.6. Algorithm 7 presents the pseudocode for hybrid filtering at a specific layer. Compared with Algorithm 1, the key differences are: (1) only examining outgoing edges within

Algorithm 7: HybridFilteringLayer

Input : $\mathbb{G}$: HSI layer; q : query vector; $[l, h]$: query range; m : number of visited neighbors per object; ep : entry point; k : number of nearest neighbors.

Output: q 's approximate k nearest neighbors within $[l, h]$.

```

1 push  $ep$  to the min-heap  $cand$  in the order of distance to  $q$ ;
2 push  $ep$  to the max-heap  $ann$  in the order of distance to  $q$ ;
3  $S \leftarrow$  segments that intersect with  $[l, h]$ ;
4 while  $|cand| > 0$  do
5    $o \leftarrow$  pop the nearest object to  $q$  in  $cand$ ;
6    $u \leftarrow$  the furthest object to  $q$  in  $ann$ ;
7   if  $\Gamma(o, q) > \Gamma(u, q)$  then break;
8   foreach  $i \in S$  do
9      $N \leftarrow$  the top- $(\lceil m/|S| \rceil)$  neighbors in  $\mathbb{G}[o][i]$ ;
10    foreach  $unvisited v \in N$  do
11      mark  $v$  as visited;
12       $u \leftarrow$  the furthest object to  $q$  in  $ann$ ;
13      if  $\Gamma(v, q) < \Gamma(u, q)$  or  $|ann| < k$  then
14        push  $v$  to  $cand$ ;
15        if  $l \leq v[A] \leq h$  then push  $v$  to  $ann$ ;
16        if  $|ann| > k$  then pop  $ann$ ;
17 return  $ann$ ;
```

intersected segments (Line 8) and (2) pushing qualified objects in the query range into the results (Line 15).

Range-aware Strategy Selection. Let Y be the cardinality of objects within a query range. Observing that pre-, post-, and hybrid filtering perform best for small-, large-, and mid-range queries, respectively, we propose the following heuristic for strategy selection: use Strategy A if $Y \leq \tau_A$, Strategy B if $Y \geq \tau_B$, and Strategy C if $\tau_A < Y < \tau_B$. Here, τ_A and τ_B are thresholds distinguishing the optimal ranges for each strategy, derived from historical data analysis. Given these thresholds, we estimate the cardinality of an incoming query to apply the heuristic. Since statistic collection and cardinality estimation are well studied [12, 27] and not the focus of this paper, we provide a simple preprocessing method to validate our heuristic. Specifically, we sample objects from the base dataset as queries and assign each a random query range. We then execute these queries using the three strategies and record recall and latency metrics. Given a recall target, we analyze records meeting this requirement and identify two turning points where pre- and post-filtering outperform hybrid filtering. These points establish τ_A and τ_B , guiding strategy selection for future queries.

4.3 Theoretical Analysis

Space Complexity. Following HNSW [23], we use a 32-bit integer to store each edge in HSI and analyze space complexity using 32-bit as a storage unit. In HSI, each node has up to MS edges (taking MS units), a bitmap of size MS (taking $\frac{MS}{32}$ units), and a skip list connection (taking one unit). For a dataset of n objects, HSI contains nL' nodes, where L' is the average number of levels. This results in an expected space complexity of $O(nL'(\frac{33}{32}MS + 1))$. As discussed in [23], the average number of levels in HNSW is

Table 1: Dataset specifications

Dataset	Dimension	#Base	#Query	Type
SIFT1M	128	1,000,000	1,000	Image + Attributes
GIST1M	960	1,000,000	1,000	Image + Attributes
GloVe	100	1,183,514	1,000	Text + Attributes
Msong	420	992,272	200	Audio + Attributes
WIT-Image	2048	1,000,000	1,000	Image + Attributes
Paper	200	2,029,997	10,000	Text + Attributes

a constant, and since HSIG uses the same strategy to determine the number of levels, L' is also a constant in HSIG. S and M are experimentally determined and are generally small constants. Given that L' , S , and M are all considered small constants relative to n , the space complexity can be simplified to $O(n)$.

Construction Complexity. Consider a dataset with n objects divided into S subsets, each containing $n_1, n_2, \dots, n_S$ objects. Inserting an object into HSIG requires three operations: (OP1) backbone graph insertion, (OP2) skip list insertion, and (OP3) edge masking. OP3 runs in constant time, while OP2 has an expected complexity of $O(\log n)$ [32]. OP1 performs ANNS on the HNSW of each segment, requiring S ANNS iterations. Since ANNS on an HNSW with x objects takes $O(\log x)$ time, OP1 costs $\sum_{i=1}^S \log(n_i)$ bounded by $S \log n$, making OP1 an $O(S \log n)$ operation. Neglecting constants, the expected complexity of inserting an object is $O(\log n)$, and constructing an HSIG for n objects scales as $O(n \log n)$.

Search Complexity. The complexity scaling of a single search can be strictly analyzed under the assumption that HSIG exactly guarantees inclusivity with respect to HNSW. For an HSIG with n objects, consider a query range covering Y objects and a small constant k negligible compared to n . The search complexities of the three strategies in HSIG are as follows:

A. Pre-Filtering. Searching the skip list has an expected complexity of $O(\log n)$ [32], and computing vector distances within the query range takes $O(Y)$ time. Thus, the total complexity is $O(Y + \log n)$. Due to range-aware search in HSIG, Pre-Filtering is used only when Y is smaller than a constant τ_A , ensuring it typically operates with an $O(\log n)$ complexity.

B. Post-Filtering. This strategy involves searching the global HNSW, which has an expected time complexity of $O(\log n)$ [23, 41].

C. Hybrid Filtering. For RF-ANNS, hybrid filtering selects segments covering the query range and performs ANNS on their HNSWs. Let n' be the number of objects in the intersected segments, searching the HNSW takes $O(\log n')$ time. Since $n' \leq n$, the expected time complexity is $O(\log n)$. Although the theoretical complexity is derived under the exact inclusivity assumption, experimental results (Section 5.8) confirm the method’s logarithmic scaling with data size, validating its efficiency and scalability.

5 EXPERIMENT

5.1 Experimental Setup

Datasets. We use six real-world datasets of varying sizes and dimensions. The Paper [40] and WIT-Image [52] datasets include both feature vectors and attributes. The Paper contains publication,

topic, and affiliation attributes, which we convert from categorical to numerical, while WIT-Image uses image size as its attribute. For the remaining datasets, which contain only feature vectors, we generate numerical attributes using a method similar to [39], assigning each vector a random value between 0 and 10,000. The dataset characteristics are detailed in Table 1. For each query, we generate a query range uniformly between 0.1% and 100%.

Compared Methods. We compare HSIG against six competitors in terms of RF-ANNS performance:

- **ADBV** [43] is a hybrid analytic engine developed by Alibaba. It enhances PQ [16] for hybrid ANNS and proposes the accuracy-aware, cost-based optimization to generate optimal execution plans.
- **Milvus** [39] partitions datasets based on commonly utilized attributes and implements ADBV within each subset.
- **NHQ** [40] constructs a composite graph index based on the fusion distance of vectors and attributes for hybrid queries. It proposes enhanced edge selection and routing mechanisms to boost query performance.
- **NGT** [46] is an ANNS library developed by Yahoo Japan that processes hybrid queries using the post-filtering strategy.
- **Vearch** [17, 20] is a high-dimensional vector retrieval system developed by Jingdong that supports hybrid queries through the post-filtering strategy.
- **SeRF** [52] designs a 2D segment graph that compresses multiple ANNS indexes for half-bounded range queries and extends this to support general range queries.

We use the Euclidean distance function to measure vector distances.

Metrics. We evaluate query effectiveness by recall and efficiency by measuring the number of queries processed per second (QPS).

Parameter Settings. The parameters S , M , and $efCons$ represent the number of segments, maximum edge connections, and candidate neighbors during index construction, respectively. We use grid search to determine their optimal values, setting S , M , and $efCons$ to 8, 16, and 500, respectively. The parameters m and ef relate to the search process, where m is the total number of neighbors visited per object, and ef is the number of candidates searched during a query. We vary m and ef to generate recall/QPS curves and apply grid search to set baseline parameters.

Implementation Settings. We implement HSIG construction and search algorithms based on hnsplib [23]. The code is written in C++ and compiled with GCC 10.3.1 using the "-O3" optimization flag. A Python interface is provided for the indexing library, and experiments are conducted using Python 3.8.17.

Environment. Scalability experiments are conducted on Alibaba Cloud Linux 3.2104 LTS with 40 cores and 512GB memory. Other experiments are conducted on a Linux server with an Intel(R) Xeon(R) E5-2609 v3 (1.90GHz, 6 cores), 16GB memory, and Ubuntu 18.04.5.

5.2 Overall Performance

We evaluate the query performance of HSIG and its competitors with k values of 10 and 100. Based on the preprocessing method in Section 4.2, we set τ_A and τ_B to 1% and 50% of the dataset size. Figure 5 shows query performance, while Table 2 presents index sizes and build times. Although HSIG does not excel in index size or build time due to its multi-segment structure and extensive edge

Table 2: Index build time and index size.

Method	Build Time (s)						Index Size (MB)					
	SIFT1M	GIST1M	GloVe	Msong	WIT-Image	Paper	SIFT1M	GIST1M	GloVe	Msong	WIT-Image	Paper
Vearch	735	1319	1187	2241	1294	617	692	3905	741	2095	4456	2430
NGT	789	27357	15281	771	8620	814	764	4031	773	1894	4277	2129
NHQ	2806	1689	4956	841	889	5039	78	66	52	99	97	158
ADBV	860	4318	896	2069	10039	2444	21	24	25	22	24	43
Milvus	1459	6931	1560	4289	4983	2477	30	52	35	36	56	61
SeRF	2502	11820	2678	4817	13440	6189	763	3896	704	1852	4185	2096
HSIG	2406	10827	2601	4230	16076	6254	1554	4728	1713	2647	5008	3785

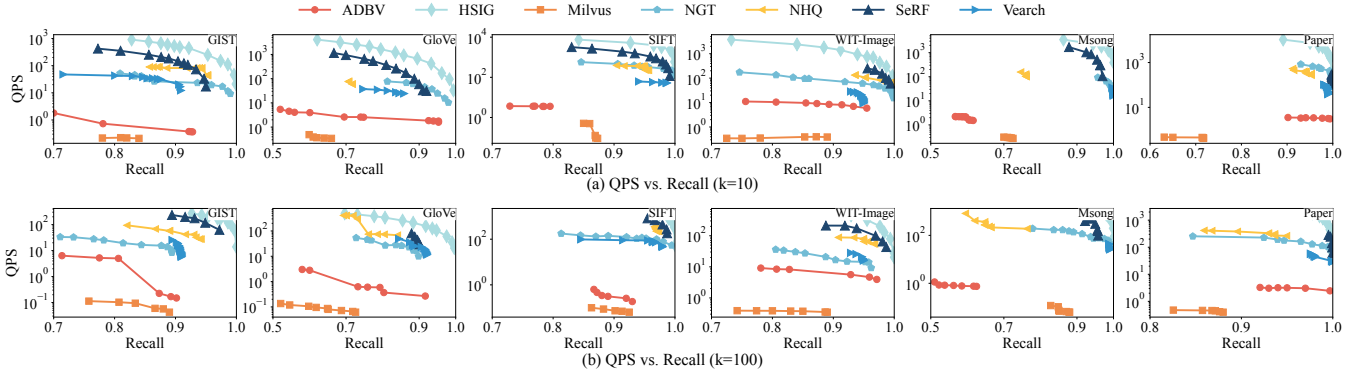


Figure 5: Overall Performance.

connections, it is comparable to SeRF, the state-of-the-art PG-based solution for RF-ANNS. PQ-based methods like ADBV and Milvus are space-efficient but struggle with query accuracy and efficiency compared to PG-based methods. As shown in Figure 5, HSIG consistently outperforms baselines across all datasets regarding the QPS vs. recall trade-off. For example, with $k = 10$ and a recall of around 0.9, HSIG achieves a QPS two orders of magnitude higher than ADBV on the GloVe and GIST1M datasets, one order of magnitude higher than NHQ on the SIFT1M dataset, and outperforms SeRF by up to 2.29 times across all datasets. These results highlight HSIG’s effectiveness, benefiting from its unified graph structure and range-aware strategy selection. Additionally, HSIG allows HNSW reconstruction with varying edge degrees using the parameter m , whereas SeRF reconstructs HNSW with a fixed edge degree, limiting its query performance. Finally, HSIG outperforms NGT, Vearch, and NHQ, as they employ the post-filtering strategy and perform poorly on small query ranges.

5.3 Effect of Range-aware Search Strategy Selection

We evaluate HSIG’s performance across small, medium, and large query ranges. The methods compared are as follows: (1) **HSIG-pre** uses HSIG with the pre-filtering strategy. (2) **PQ-pre** performs attribute filtering first, followed by PQ-based vector retrieval. (3) **Btree-pre** uses a B-tree for attribute filtering, followed by brute-force vector retrieval. (4) **HSIG-post** applies HSIG with the post-filtering strategy. (5) **HNSW-post** builds HNSW over the entire

dataset and applies the post-filtering strategy. (6) **HSIG-hybrid** employs HSIG for RF-ANNS queries using the hybrid filtering strategy. (7) **SeRF** is a state-of-the-art RF-ANNS solution that uses a hybrid filtering. (8) **HSIG-range-aware** uses HSIG with range-aware search strategy selection. (9) **Dedicated** builds specialized indexes for each strategy, with Btree-pre, HNSW-post, and SeRF used for pre-, post-, and hybrid filtering, respectively, and selects the best strategy based on query range.

The results are shown in Figure 6. Some methods have missing QPS values for specific query ranges, indicating they could not meet the recall threshold. HSIG-pre, HSIG-hybrid, and HSIG-post outperform competitors in small, medium, and large ranges, respectively. For example, HSIG-pre outperforms Btree-pre by 20.3% at a recall of 0.9 in small query ranges. HSIG-hybrid exceeds SeRF by 1.21 times in medium query ranges at a recall of 0.95. HSIG-post surpasses HNSW-post by 37.5% at a recall of 0.99 in large query ranges. Additionally, HSIG-pre outperforms HSIG-hybrid and HSIG-post in small ranges, HSIG-post surpasses HSIG-hybrid and HSIG-pre in large ranges, and HSIG-hybrid performs best among the three strategies in medium ranges, validating our range-aware heuristics. Finally, HSIG-range-aware consistently outperforms Dedicated by up to 1.1 times across all query ranges, thanks to its unified PG-based index and range-aware strategy selection.

5.4 Validation of Inclusivity of HSIG

We evaluate HSIG’s inclusivity using the inclusiveness metric. Inclusiveness is computed as $\frac{\text{\#common-edge}}{\text{\#hnsw-edge}} \times 100\%$, where $\text{\#common-edge}$

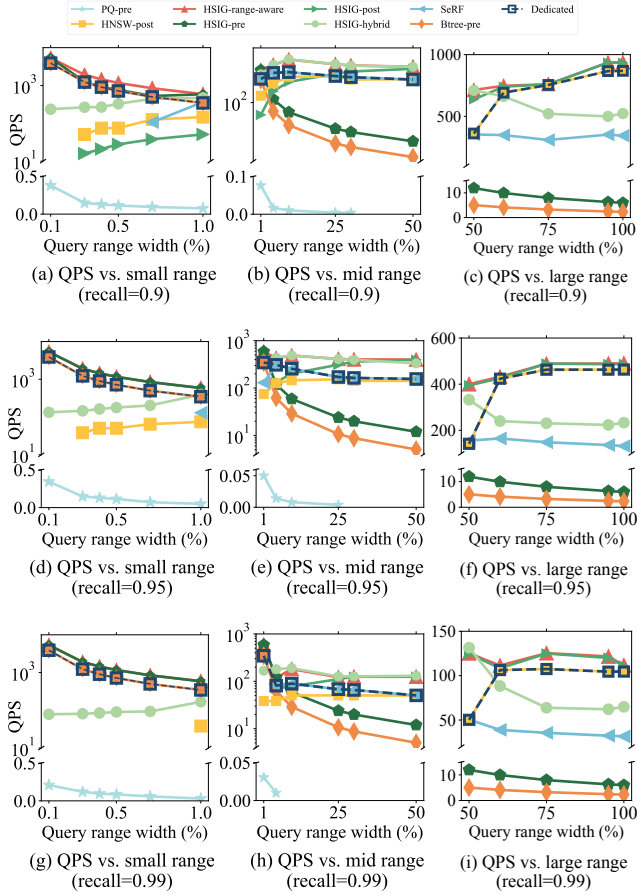


Figure 6: Impact of different query ranges on GloVe dataset.

is the number of identical edge connections in both HSIG and the multi-segment HNSW (where multi-segment HNSW refers to the HNSW constructed for any combination of segments), and $\#hns\text{-}edge$ is the total number of edges in the multi-segment HNSW. According to Definition 2, the multi-segment HNSW should be a sub-graph of HSIG to satisfy inclusivity. Thus, 100% inclusiveness indicates that HSIG strictly satisfies inclusivity. In this experiment, we partition the dataset evenly into eight segments and construct HNSWs for 1, 2, 4, 6, and 8 contiguous segments. Figure 7 shows that the average inclusiveness of HSIG exceeds 80%, demonstrating that HSIG achieves significant inclusiveness and approximately satisfies inclusivity.

To further evaluate the impact of inclusivity on query performance, we compare HSIG at varying levels of inclusiveness (30%, 40%, 60%, and 80%) against two competitive methods that guarantee exact inclusivity. The first method, *Optimal HNSW*, builds an HNSW in real time for objects within each query range. The second method, *MS-HNSW*, pre-builds HNSWs for each segment. During the search, *MS-HNSW* identifies the segments intersecting with the query range, retrieves vectors from the corresponding HNSWs, and combines the intermediate results to obtain the final

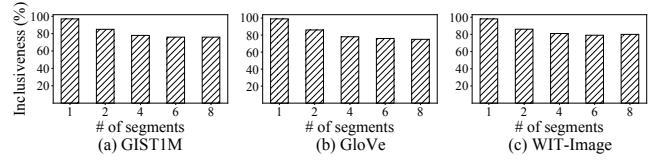


Figure 7: Inclusiveness of HSIG.

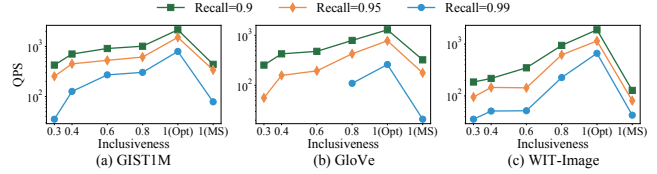


Figure 8: Impact of Inclusivity.

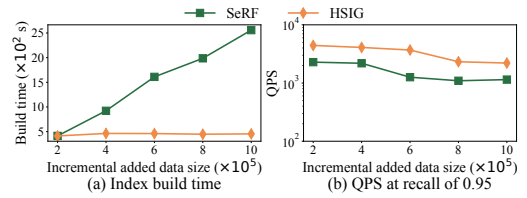


Figure 9: Performance of incremental insertion on SIFT1M.

results. The results are shown in Figure 8. While *Optimal HNSW* offers the best performance, building indexes in real time for every query is time-consuming and impractical. As HSIG’s inclusiveness increases, its query performance improves, approaching that of *Optimal HNSW*. Additionally, HSIG consistently outperforms *MS-HNSW*, which requires more distance computations. These results demonstrate the effectiveness of HSIG’s inclusivity, showing that higher inclusiveness leads to better query performance.

5.5 Validation of Incremental Insertion

In this section, we evaluate HSIG’s incremental insertion capability. We first build HSIG with 200,000 objects from the SIFT1M dataset, followed by four rounds of incremental insertion, each adding 200,000 objects. We compare the index build time and query performance against the state-of-the-art method SeRF. As shown in Figure 9, HSIG’s build time remains stable with each insertion since the number of inserted objects is consistent, whereas SeRF’s build time increases linearly due to its lack of incremental update support. Moreover, HSIG outperforms SeRF in query efficiency at a recall of 0.95. These results highlight HSIG’s effectiveness in supporting incremental insertions, showing that it is suitable for applications with continuously evolving data.

5.6 Validation of Runtime Neighbor Selection

In this section, we compare two strategies for runtime neighbor selection in hybrid filtering, as described in Section 4.2. The first strategy, Hybrid-S1, computes the distance to neighbors in all S' segments (assuming there are S' segments intersecting with the

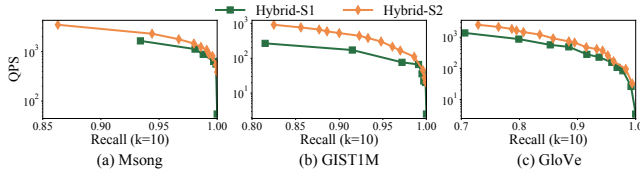


Figure 10: Impact of the runtime neighbor selection method.

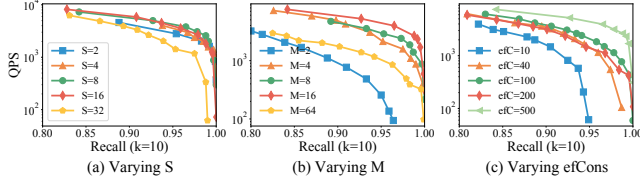


Figure 11: Performance of index parameters on SIFT1M.

query range) and then selects the top- m neighbors by sorting them based on their distances. The second strategy, Hybrid-S2, selects the top- $(\lceil m/S' \rceil)$ neighbors from each segment. As shown in Figure 10, Hybrid-S2 outperforms Hybrid-S1 in query efficiency. This is because Hybrid-S2 selects the top- $(\lceil m/S' \rceil)$ neighbors from the pre-ordered neighbor lists without additional distance calculations, as neighbors of the object v in each segment are already sorted by their distance to v upon acquisition via *ANNSearch*. In contrast, Hybrid-S1 requires calculating distances for all neighbors across S' segments, increasing query time. Therefore, we adopt Hybrid-S2 as the default runtime neighbor selection method.

5.7 Parameter Study

Impact of Index Construction Parameters. We analyze the sensitivity of three parameters in HSIQ construction: S , M , and $efCons$. Figures 11 and 12 show how parameters affect query performance and index build times, respectively. Figure 11a shows the impact of varying S on query performance, with a performance increase from 2 to 8, followed by a decline as S grows further due to increased neighbor visits. Figure 11b and Figure 11c illustrate the effects of varying M and $efCons$ on query performance. Lower M degrades graph quality, while higher M increases the number of objects traversed during the search. Similarly, lower $efCons$ leads to insufficient candidates, whereas higher $efCons$ includes irrelevant candidates, both hindering query performance. Therefore, setting these parameters based on the dataset and workload is crucial for balancing query efficiency and accuracy. As shown in Figure 12, index build time rises with higher S , M , and $efCons$ due to increased distance computations. Based on a comprehensive evaluation of query performance and index construction time, we select $S = 8$, $M = 16$, and $efCons = 500$ as default settings.

Impact of Search Parameters. Figure 13 shows the impact of varying the parameters ef and m on hybrid filtering in HSIQ. Here, ef is typically set to a value greater than k . Figure 13a and Figure 13c show that with $m = 16$, as ef increases, recall gradually improves while QPS decreases. This occurs because a larger ef

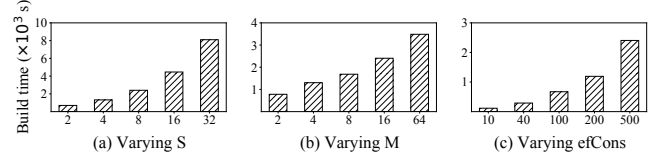


Figure 12: Index build time on different index parameters.

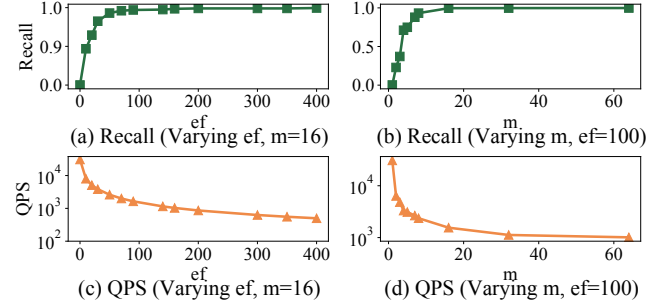


Figure 13: Performance on different search parameters.

requires visiting more objects to gather sufficient candidates, enhancing accuracy but reducing efficiency. Figure 13b and Figure 13d show that with $ef = 100$, increasing m leads to a gradual improvement in recall but a decrease in query efficiency. This is because a larger m results in visiting more neighbors of each object during the search, improving accuracy but at the cost of efficiency.

Impact of k values. Figure 14 shows the impact of different k values on query performance of HSIQ. HSIQ maintains strong efficiency and accuracy across various k values. However, as k increases from 10 to 100, performance gradually declines due to the increased number of candidates that need to be filtered during the search.

5.8 Scalability

We evaluate the scalability of HSIQ using datasets ranging from 10 to 100 million objects. We fix the index parameters to $S = 8$, $M = 16$, and $efCons = 500$, and maintain a query range width of 25%. As shown in Figure 15, both the index size and build time increase almost linearly with the dataset size. Figure 15c plots the hybrid filtering latency versus data size, indicating a logarithmic search complexity. Notably, the recall consistently reaches 0.99 across all dataset sizes. These results demonstrate that HSIQ achieves strong scalability in both index construction and query processing.

5.9 Discussions

Range-aware strategy selection. As mentioned in Section 4.2, our range-aware strategy selection method is based on historical data statistics, not query patterns. This approach may face challenges if the data distribution of the base dataset changes significantly over time. To address this issue, we propose an adaptive method that can detect changes in data distribution. If the change exceeds the user-defined threshold, the method resamples objects from the updated base dataset to recalibrate τ_A and τ_B , thereby adjusting the range-aware search strategy selection.

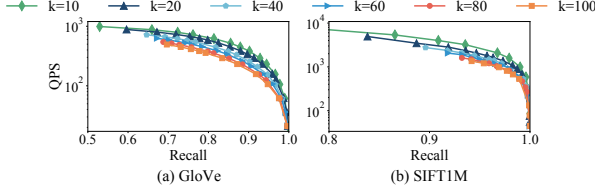


Figure 14: Performance of different k values.

RF-ANNS with Multiple Attributes. Existing PG-based indexes struggle to support RF-ANNS queries with multiple attributes, as incorporating multiple attributes into a graph is challenging. However, with two enhancements, HSIG can be extended to handle such queries. While we use the case with two attributes in this discussion, the method can be adapted for more attributes. (1) Multiple single-attribute indexes: Build a separate HSIG for each attribute. For a conjunctive query with a query vector q , retrieve objects that satisfy $r_1(A_1)$ AND $r_2(A_2)$, where $r_1(A_1)$ and $r_2(A_2)$ are the attribute ranges. We aim to return the top- k ANN of q among objects satisfying both ranges. Specifically, we modify Line 15 of Algorithm 7 to "if v satisfies $r_1(A_1)$ AND $r_2(A_2)$, then push v to ann ". For disjunctive queries ($r_1(A_1)$ OR $r_2(A_2)$), we use separate indexes for A_1 and A_2 and merge the results. (2) Single index for multiple attributes: Create a composite attribute (A_1, A_2) and apply the z-order method [28] to map them into a one-dimensional attribute, enabling the construction of a single HSIG to handle RF-ANNS queries with multiple attributes. We plan to explore a dedicated algorithm for RF-ANNS queries with multiple attributes in future work.

6 RELATED WORK

6.1 ANNS

The primary approaches for k NNS can be categorized tree-based methods [2, 26], hash-based methods [13, 37, 50], quantization-based methods [1, 9, 22, 24], and PG-based methods [6, 7, 23, 34, 35, 41, 49]. Tree-structured indexes like the KD-tree [4], R-tree [11], VP-tree [8], and KMeans-tree [48] suffer from the "curse of dimensionality" [14], making them ineffective in high-dimensional spaces. Hash-based methods utilize hash functions to map vectors into hash buckets. However, as the binary hash code length increases, the number of buckets grows exponentially, leading to many empty buckets, which reduces the search accuracy. Quantization-based methods reduce storage and computational costs but involve lossy compression, which produces a "ceiling" phenomenon on the search accuracy [21]. PG-based methods show significant performance advantages and have attracted substantial attention. However, while effective for vector retrieval, these methods fail to handle attribute filtering effectively, limiting their applicability in scenarios requiring integrated vector retrieval and attribute filtering.

6.2 Filtered ANNS

Most hybrid k NNS queries separate the process into vector retrieval and attribute filtering, which are combined to produce final results. MA-NSW [45] explores ANNS with attribute constraints by constructing indexes for each attribute combination. Vearch

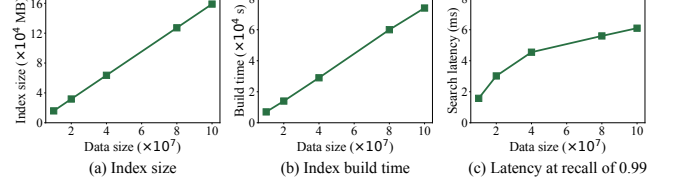


Figure 15: Impact of varying data size on SIFT dataset.

[20] and NGT [46] apply post-filtering, which first retrieves candidates through vector search and then filters candidates based on the attributes. This strategy is extendable to some vector libraries, such as Faiss [18] and SPTAG [5]. However, they perform worse when the selectivity of the query range is low, limiting the query efficiency and accuracy. ADBV [43] uses a B-tree for attributes and a PQ index for vectors, optimizing query plans with a cost model. Milvus [39] partitions datasets by attributes and adopts the query strategies of ADBV. However, they focus on query optimization and partitioning techniques without enhancing the index structure. Filtered-DiskANN [10] develops a graph supporting attribute matching and vector similarity searches. However, it focuses on attribute matching, leaving a gap for k NN with range constraints. NHQ [40] and HQANN [44] introduce a fused distance metric that combines attributes and vectors, enabling simultaneous attribute filtering and vector retrieval within a single graph index. However, they lack a solid theoretical foundation due to the irrelevance of attributes and vectors. ARKGraph [51] builds PGs for all possible attribute range combinations and compresses the indexes. However, it requires decompression during querying, reducing query efficiency. SeRF [52] addresses range-filtering k NNs by designing a segment graph that compresses multiple indexes for half-bounded range queries and extends it to support general range queries. However, SeRF does not support online updates of new data.

7 CONCLUSION

This paper addresses RF-ANNS queries over high-dimensional vectors associated with attribute values. Existing methods, including pre-, post-, and hybrid filtering strategies, which apply attribute filtering before, after, or during the ANNS process, suffer performance degradation when query ranges shift. We propose a novel framework called UNIFY, which constructs a unified PG-based index that seamlessly supports all three strategies. Within UNIFY, we introduce SIG, enabling efficient RF-ANNS by reconstructing and searching a PG from relevant segments. Additionally, we present HSIG, a variant of SIG that incorporates a hierarchical structure inspired by HNSW, achieving logarithmic time complexity for RF-ANNS. Experimental results demonstrate that UNIFY outperforms state-of-the-art methods across varying query ranges.

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